

Welcome!



The “Control Chart and Capability 101”
webinar will begin shortly

Presented by
Matt Savage
PQ Systems



Webinar Goals



Webinar Goals



Central tendency



Variability

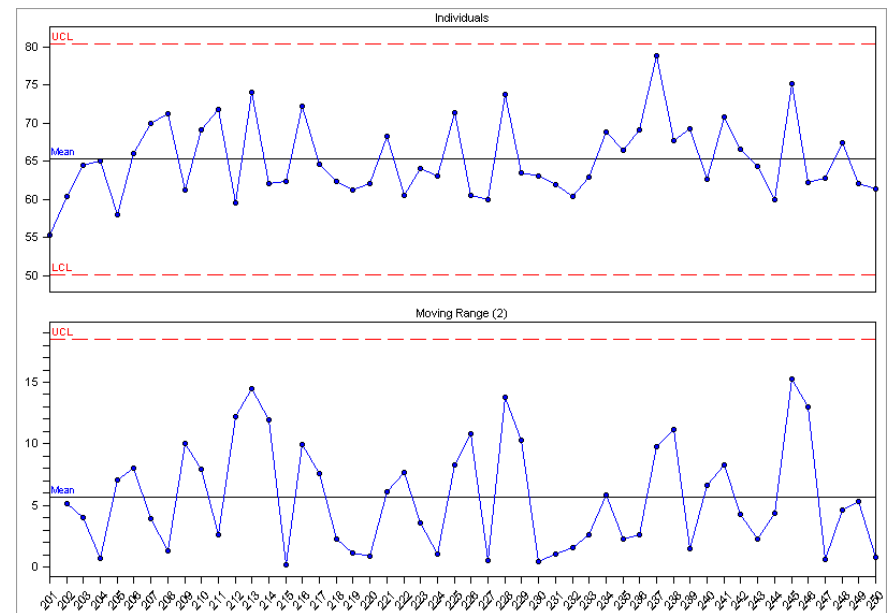
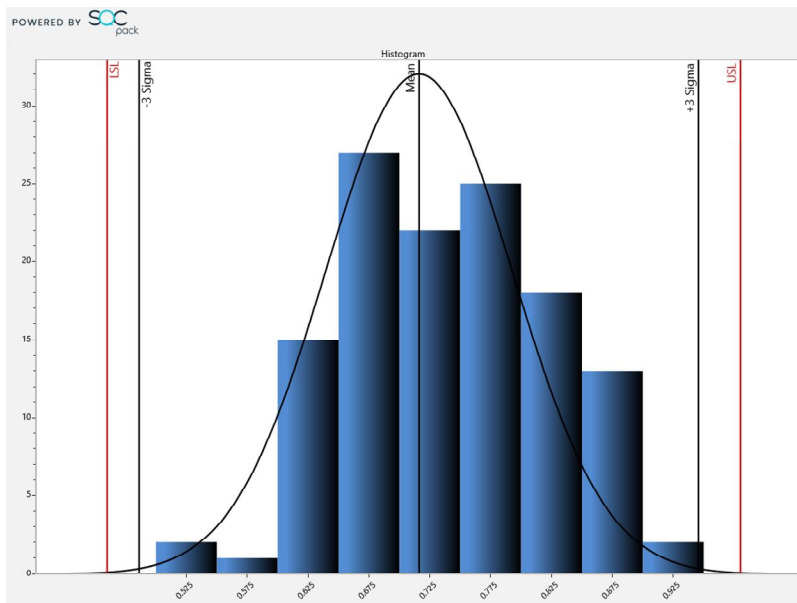
Webinar Goals



34.64 18.243 11.245 1.34 1.5 34.64 1.34
20
2.245 12.85 7.657 1.394 20 18.243
5.08 1.394 .08 2.245 5.08
10.45 6.357 1.34 17.998 34.64
36.10 .015
34.64 2.536 10.45 6.357
50.4 .08 4.698 .049 .015 18.243
17.8 15.24 7.657 15.24 .08
34.64 11.245 17.998 2.245 50.4 7.657 12.85
17.8 11.245

Data

Webinar Goals



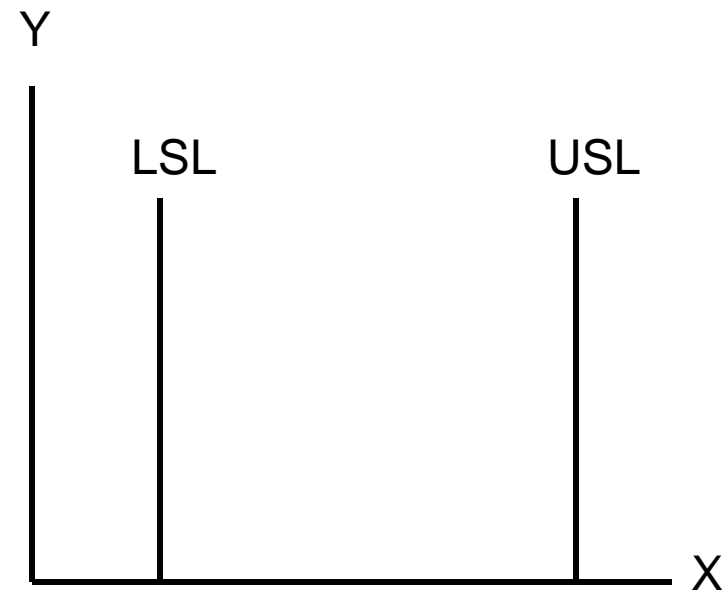
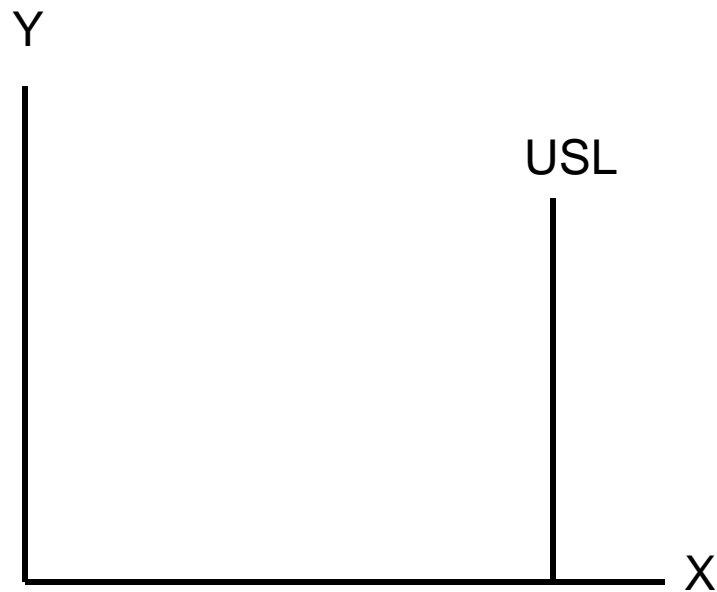
Webinar Goals



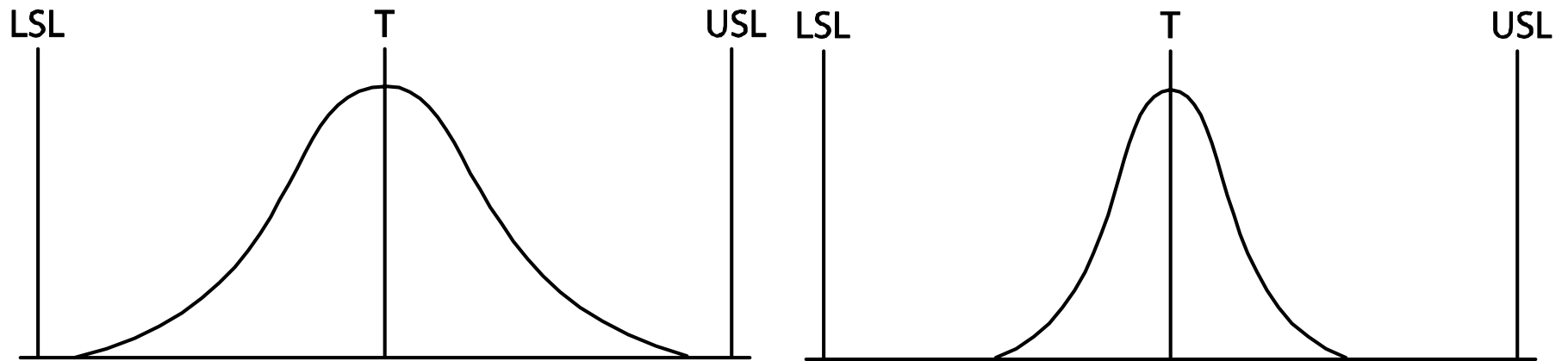
What is Capability Analysis?



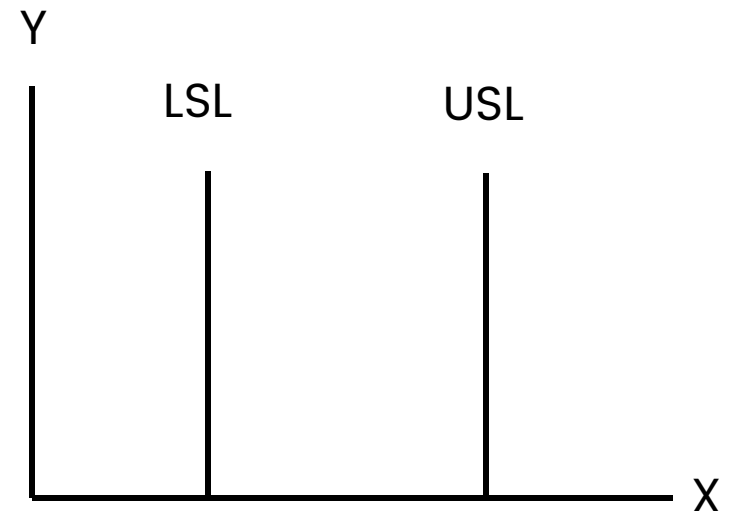
Requirement



Requirement



Control vs. Spec Limits



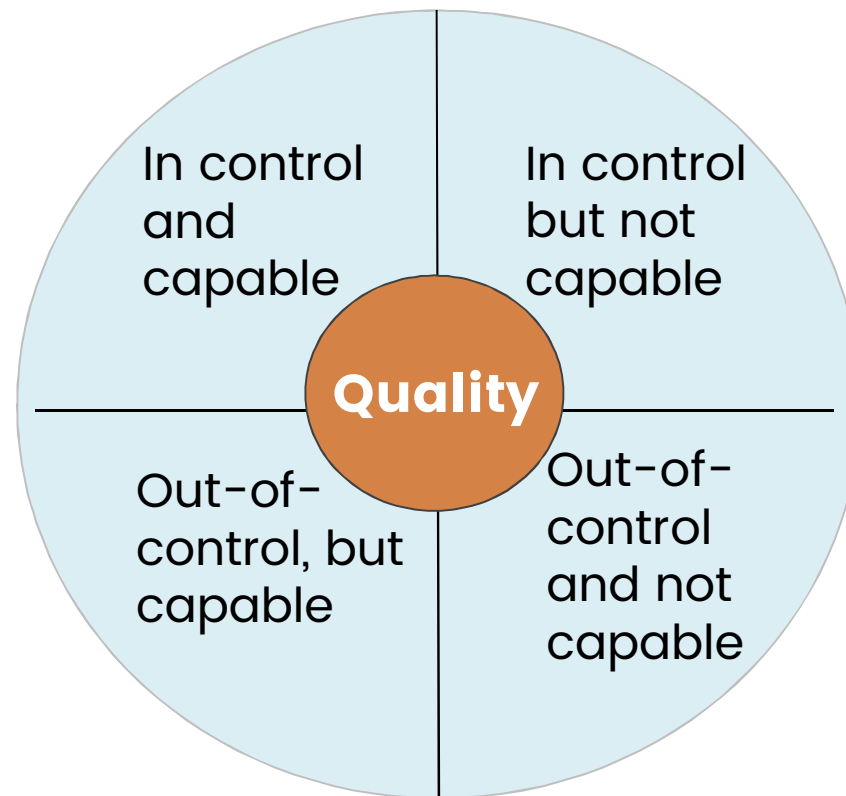
Control limits reflect **actual** process variation

Voice of the Process

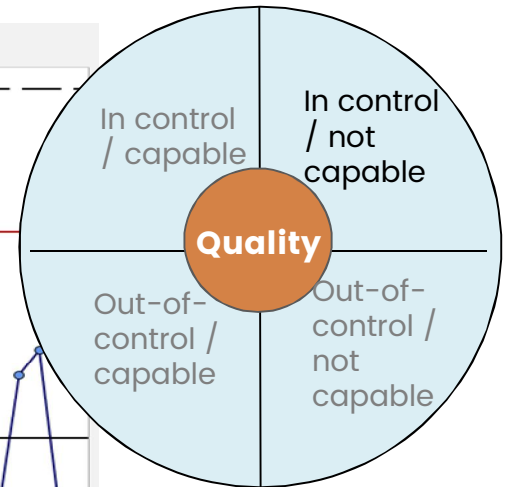
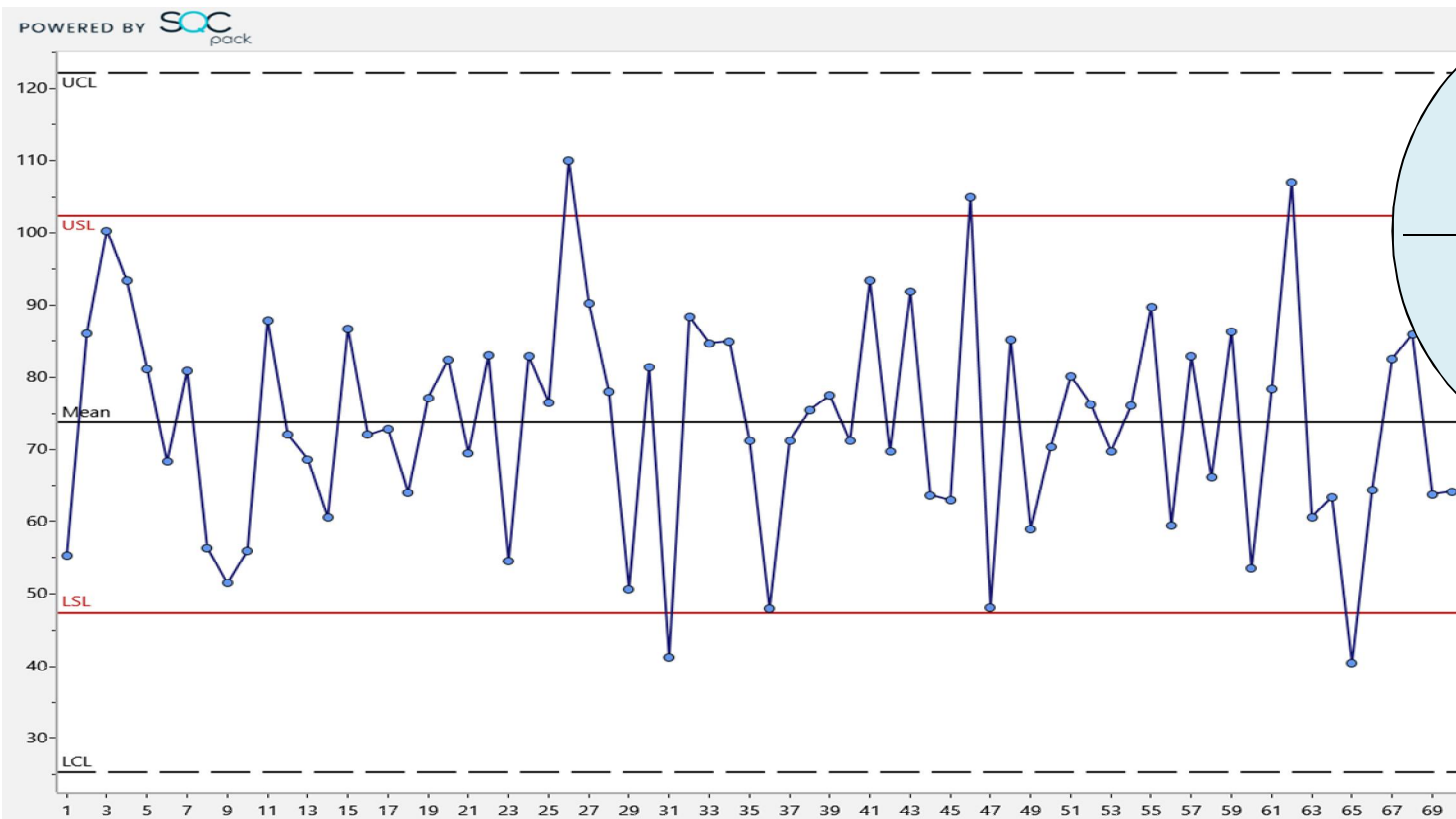
Specification limits reflect **allowable** process variation

Voice of the Customer

Four States of Quality



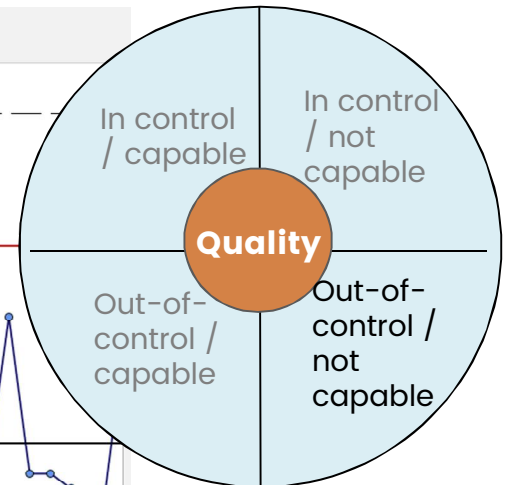
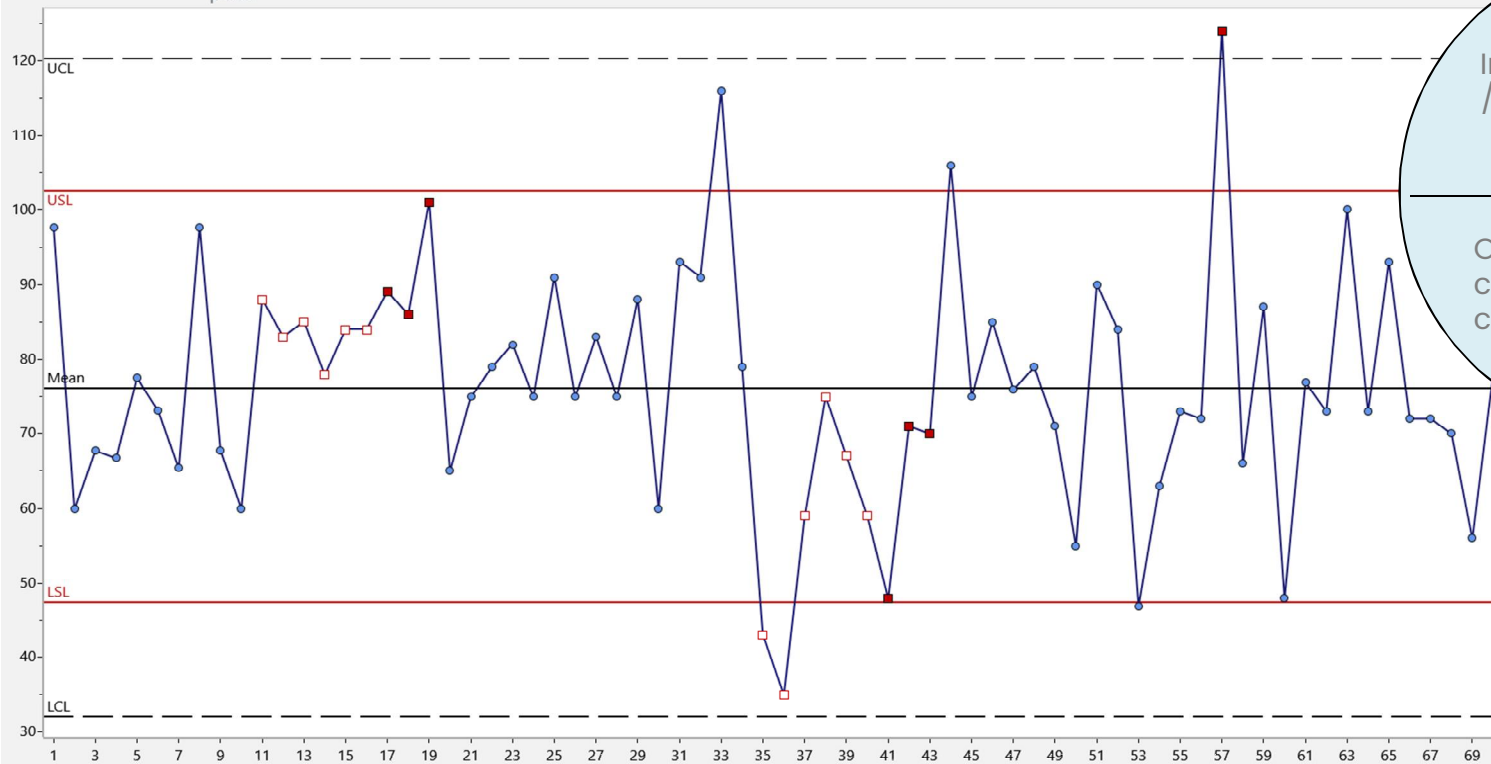
In Control & Not Capable



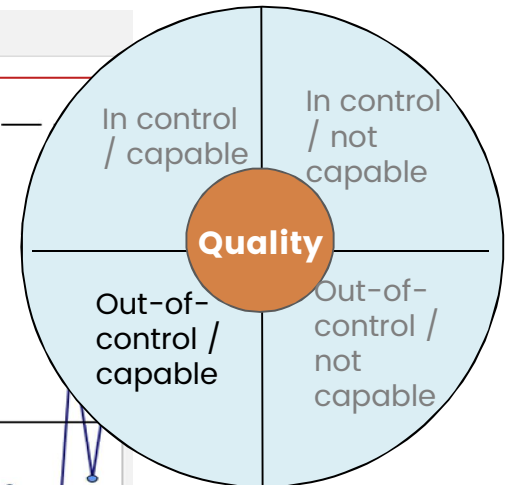
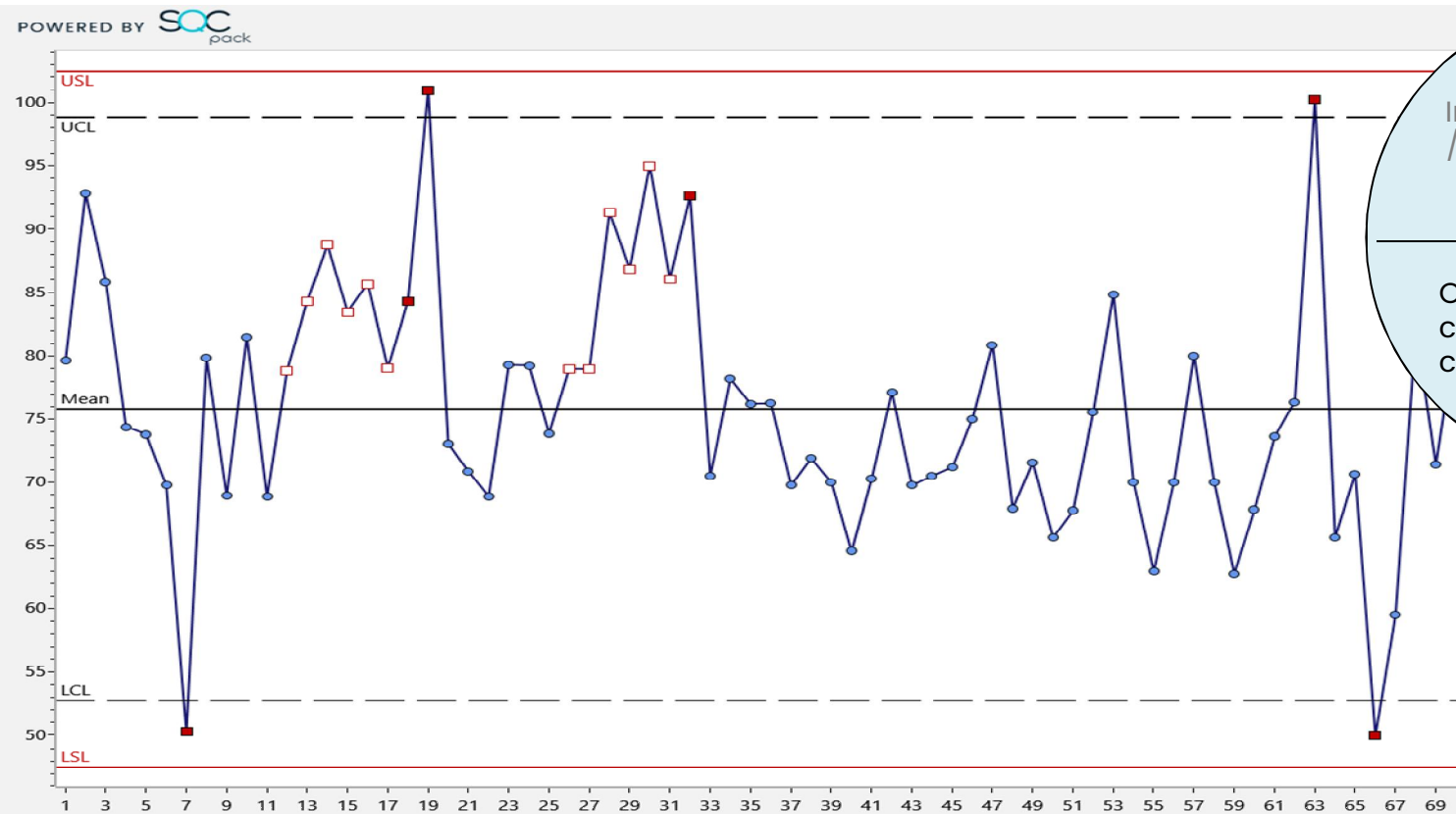
Out-of-Control & Not Capable



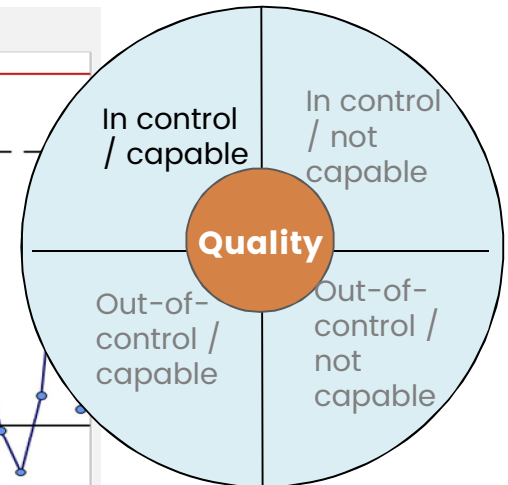
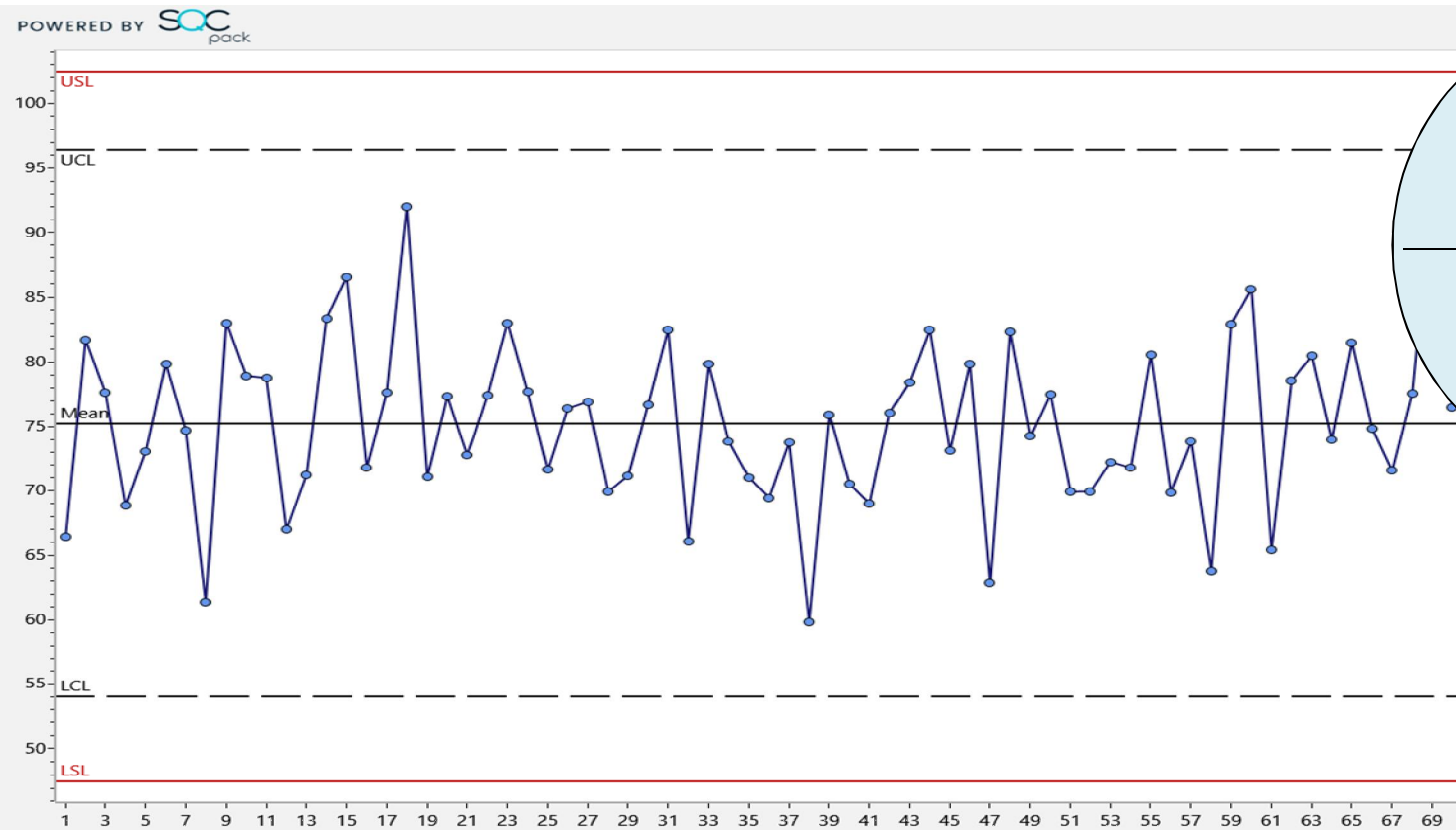
POWERED BY **SQC**
pack



Out-of-Control, but Capable



In Control & Capable



Control Charts for Count Data



**Nonconforming
or Defective**

- **p**-chart
- np-chart

**Nonconformities
or Defects**

- c-chart
- **u**-chart

Control Charts – Measurement Data



- X – Individuals
- MA – Moving average
- X-bar

- MR – Moving range
- R – Range
- S – Sigma



Purpose of Process Control



Control charts are used to:

- Determine central tendency
- Monitor variability
- Spot trends
- To determine stability and therefore predictability

Purpose of Capability Analysis



Report Card

	Last Shipment		This Shipment	
Length	A		A	
Width	C-		B	
Height	B+		A-	

Control Chart Intro / Refresher



- What is it?
- What does it look like?
- When is it used?
- How is it made?

\bar{X} -R / X-MR Control Chart



What is it?

Average / Individuals and variability

- Monitors how a system changes over time
- Monitors averages to show trends and shifts
- Monitors range to indicate changes in variation
- Used for measurement data

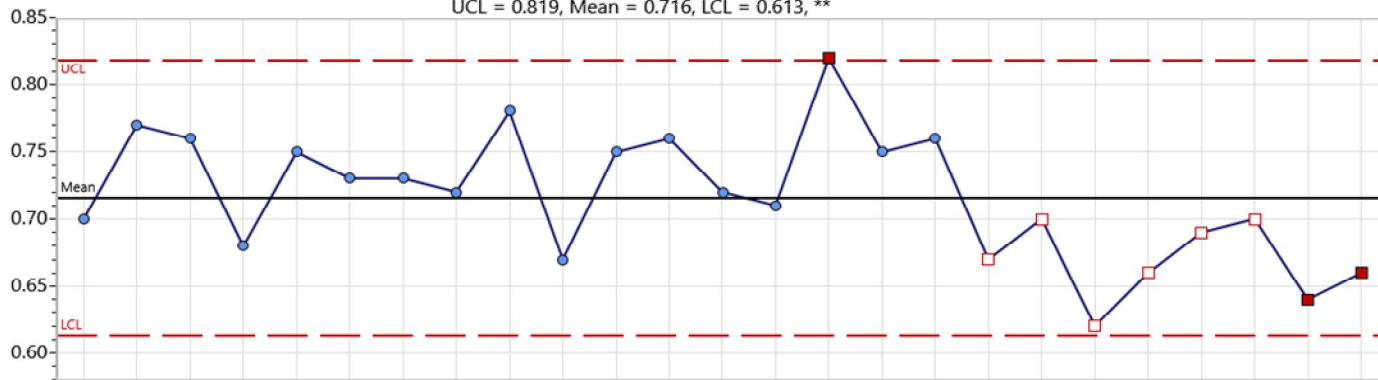
Characteristic: Gap of Dimension A

Gap of Dimension A(1)	0.65	0.75	0.75	0.60	0.70	0.60	0.75	0.60	0.65	0.60	0.80	0.85	0.70	0.65	0.90	0.75	0.75	0.75	0.65	0.60	0.50	0.60	0.80	0.65	0.65	
Gap of Dimension A(2)	0.70	0.85	0.80	0.70	0.75	0.75	0.80	0.70	0.80	0.70	0.75	0.75	0.70	0.70	0.80	0.80	0.70	0.70	0.65	0.60	0.55	0.80	0.65	0.60	0.65	
Gap of Dimension A(3)	0.65	0.75	0.80	0.70	0.65	0.75	0.65	0.80	0.85	0.60	0.90	0.85	0.75	0.85	0.80	0.75	0.85	0.60	0.85	0.65	0.65	0.65	0.65	0.75	0.65	0.60
Gap of Dimension A(4)	0.65	0.85	0.70	0.75	0.85	0.85	0.75	0.75	0.85	0.80	0.50	0.65	0.75	0.75	0.75	0.80	0.70	0.70	0.65	0.60	0.80	0.65	0.65	0.60	0.70	
Gap of Dimension A(5)	0.85	0.65	0.75	0.65	0.80	0.70	0.70	0.75	0.75	0.65	0.80	0.70	0.70	0.60	0.85	0.65	0.80	0.60	0.70	0.65	0.80	0.75	0.65	0.70	0.70	
X-bar	0.700	0.770	0.760	0.680	0.750	0.730	0.730	0.720	0.780	0.670	0.750	0.760	0.720	0.710	0.820	0.750	0.760	0.670	0.700	0.620	0.660	0.690	0.700	0.640	0.660	
Range	0.200	0.200	0.100	0.150	0.200	0.250	0.150	0.200	0.200	0.200	0.400	0.200	0.050	0.250	0.150	0.150	0.150	0.200	0.050	0.300	0.200	0.150	0.100	0.100		

X-bar

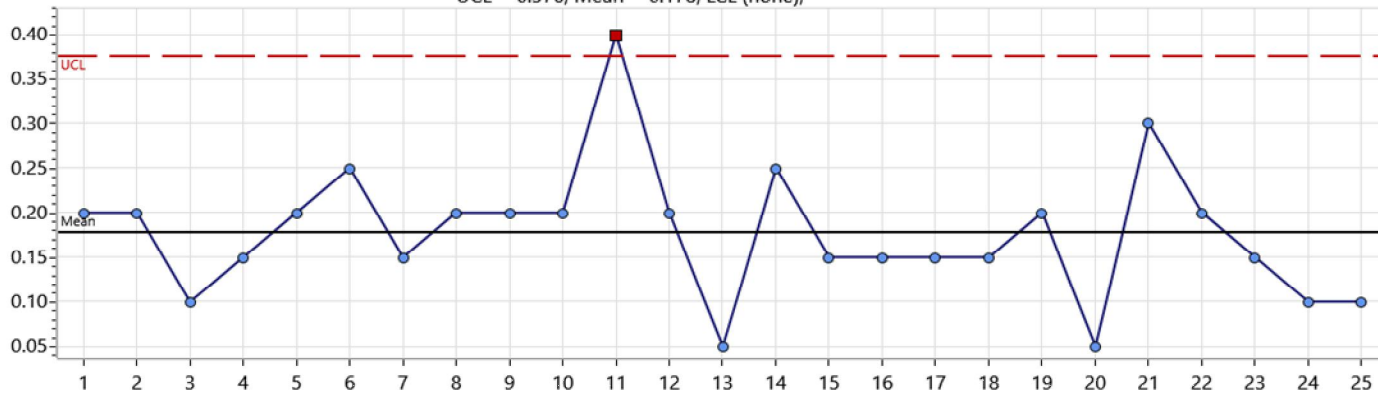
USL = 0.90, LSL = 0.50

UCL = 0.819, Mean = 0.716, LCL = 0.613, **



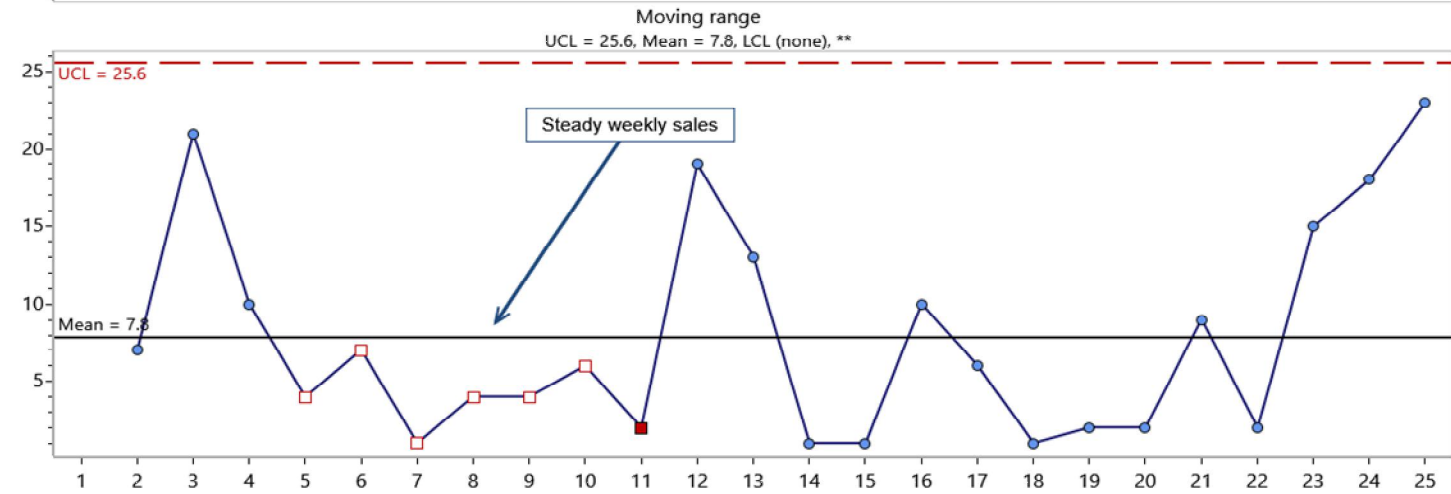
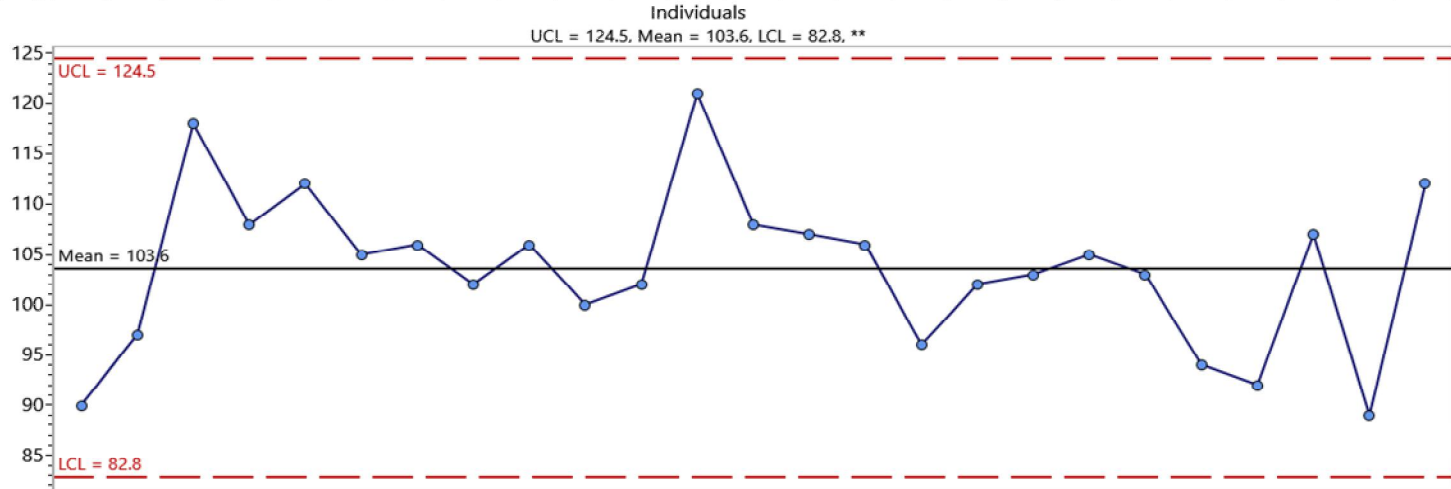
Range

UCL = 0.376, Mean = 0.178, LCL (none), **



X - MR CHART

Sales	90	97	118	108	112	105	106	102	106	100	102	121	108	107	106	96	102	103	105	103	94	92	107	89	112
Moving Range		7.0	21.0	10.0	4.0	7.0	1.0	4.0	4.0	6.0	2.0	19.0	13.0	1.0	1.0	10.0	6.0	1.0	2.0	2.0	9.0	2.0	15.0	18.0	23.0



\bar{X} -R / X-MR Control Chart



When is it used?

Answer “yes” to the following:

- Do you need to assess the variability in the system?
- Can the data be collected or does a collection of data already exist?
- Is the time order of the data preserved?
- Is the data in variables format?
- Is the data collected in an appropriate subgroups size?

\bar{X} -R / X-MR Control Chart



How is it made?

- Assumes data has been collected
 - Ideally 25 or more data points.
- Any unusual occurrences observed during data collection should have been noted.

\bar{X} -R / X-MR Control Chart



How is it made?

1. Complete the header information.
2. Record the data.
3. Calculate the statistics for each subgroup.
4. Calculate the overall averages.
5. Calculate the control limits.
6. Scale the control chart.
7. Draw the average line and control limits.
8. Plot the values on the control chart.
9. Interpret the control chart.

\bar{X} -R / X-MR Control Chart



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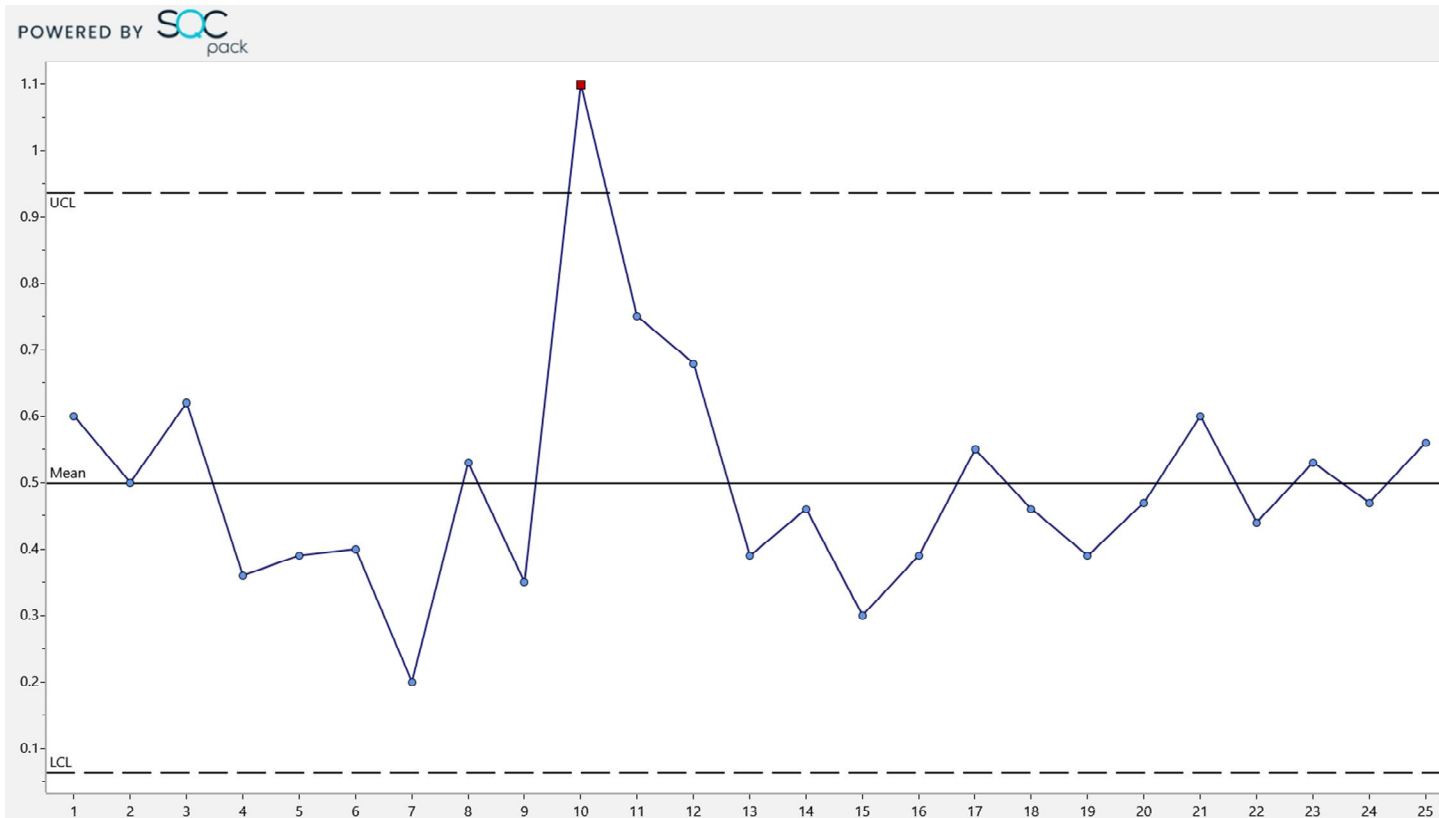
\bar{X} -R / X-MR Control Chart



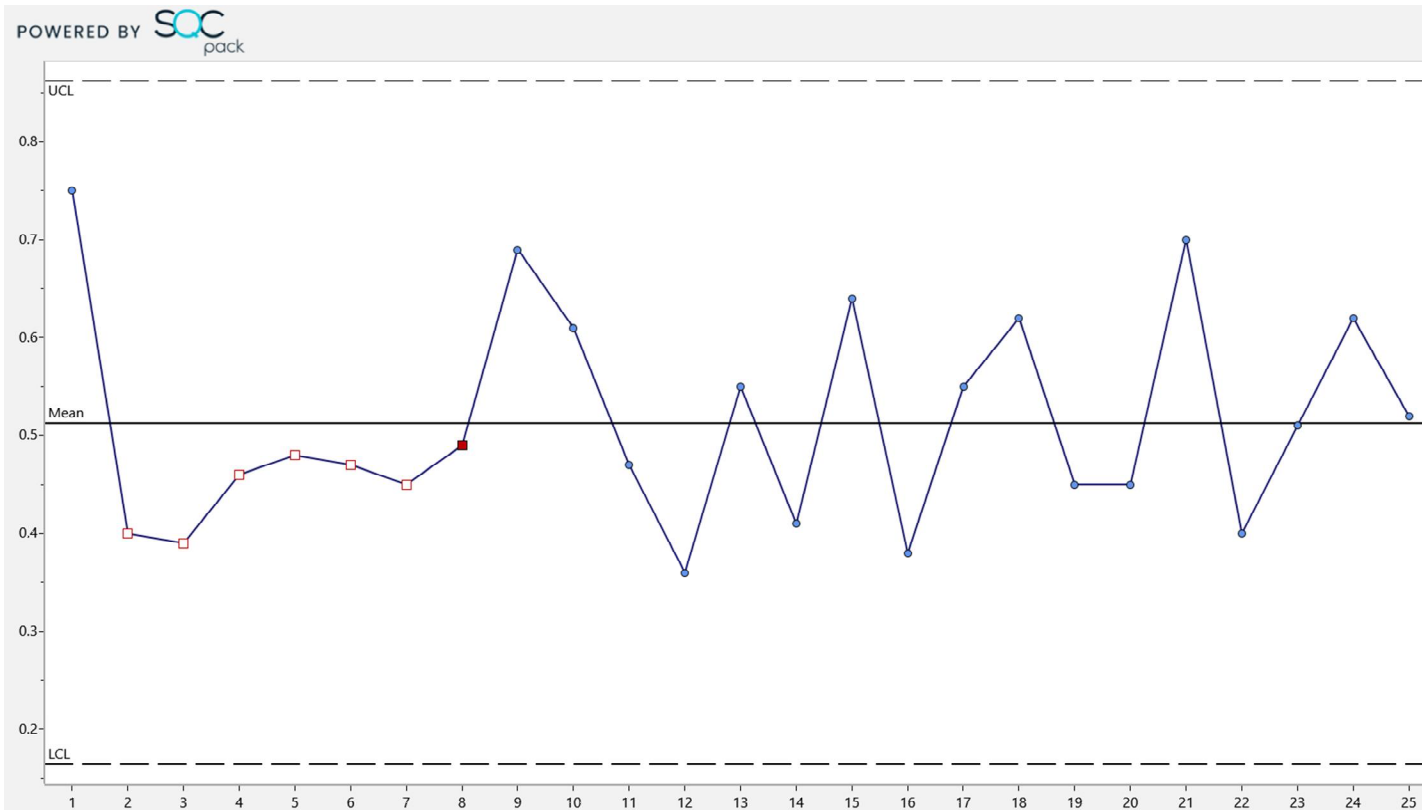
9. Interpret the control chart.

- *Basic rules for interpretation*
 - Any point lying outside the control limits.
 - Run of seven points:
 - » Seven or more points in a row above or below the center line.
 - » Seven or more points in a row going in one direction, up or down.
 - Any non-random pattern, including the following typical cases:
 - » Too close to the average.
 - » Too far from the average.
 - » Cycles.

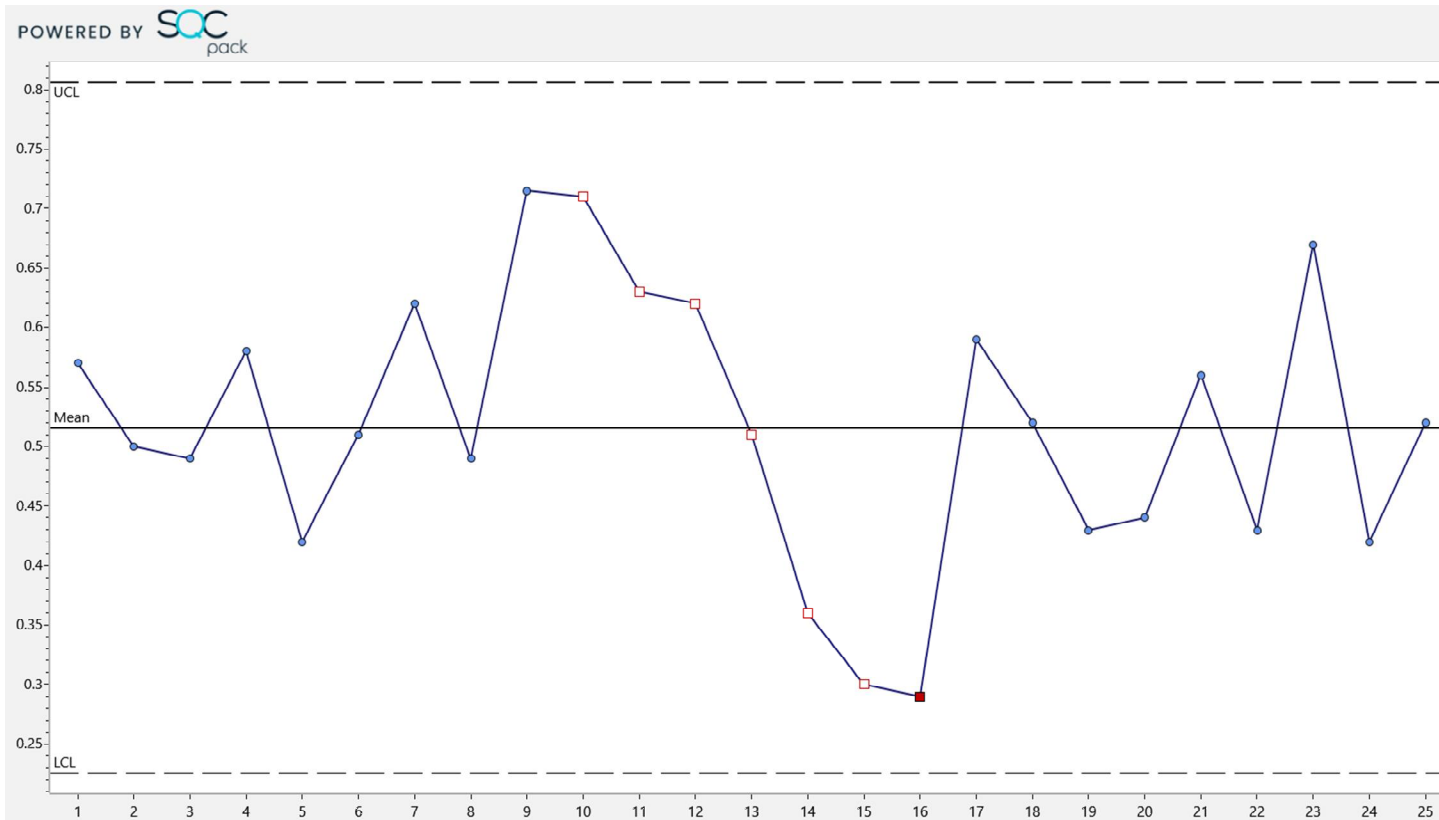
Any point beyond the control limits



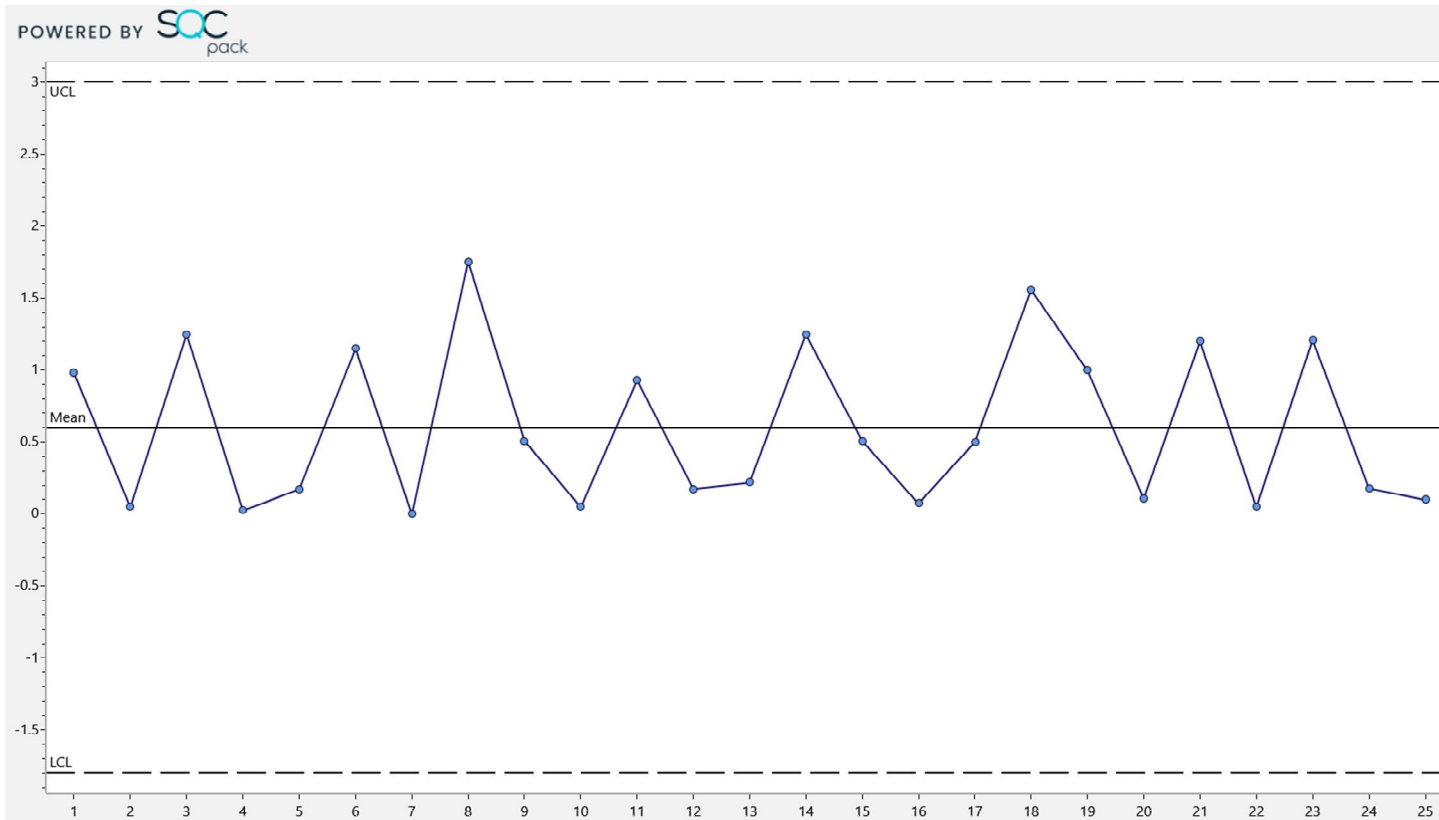
Seven consecutive below the mean



Seven consecutive decreasing



Too far from the average, cycles, ...



Tip: Use enough data



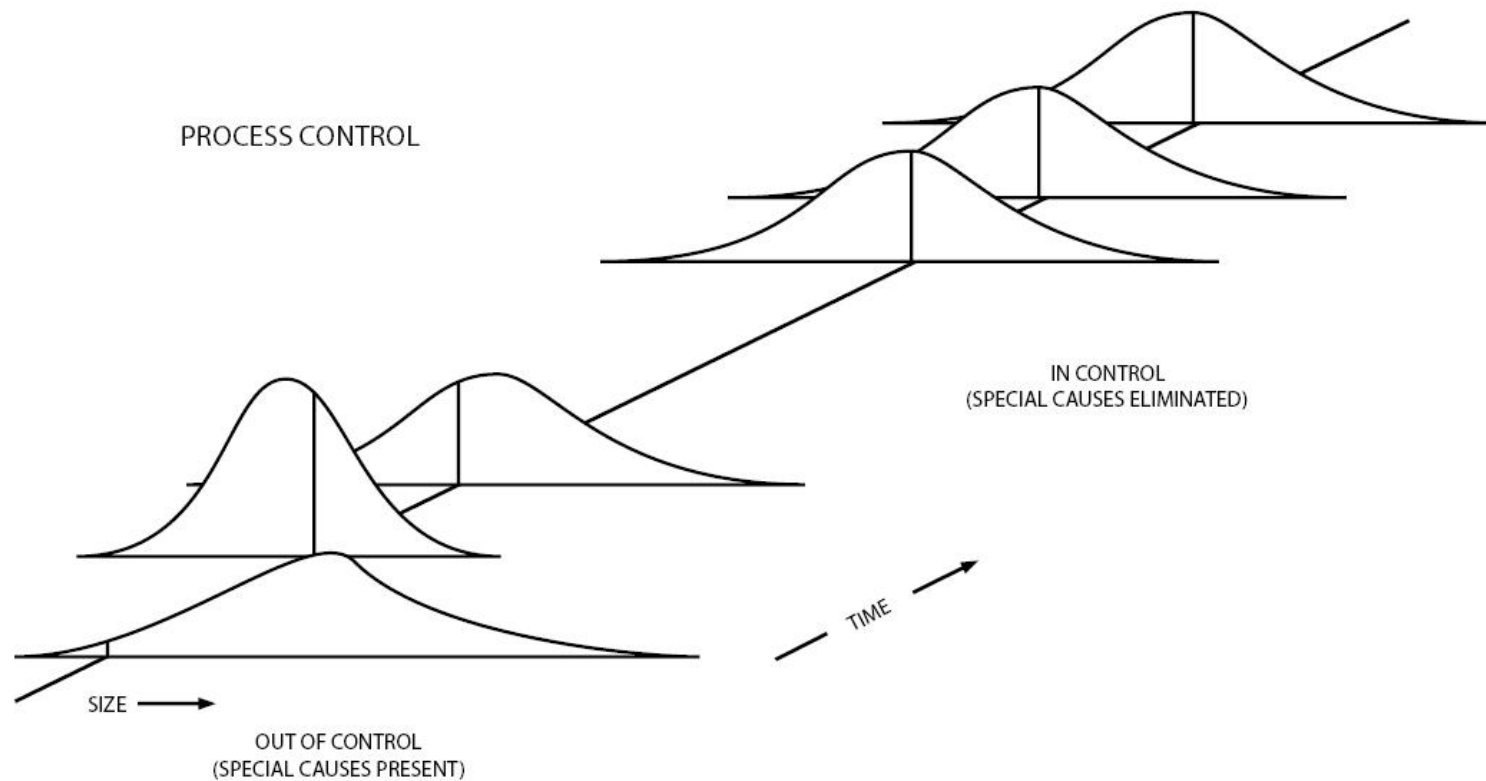
- How much data is necessary for control limits on a control chart?
- “An X-mr chart can be made with as few as four original values without an undue risk of a false alarm.” Donald J. Wheeler, Ph.D.
- Data beyond a control limit? Investigate it — even with only a few samples.

Purpose of a Control Chart

A magnifying glass with a black handle and a silver rim is positioned over a document with faint, illegible text. The word 'CLUES' is written in large, bold, red capital letters across the center of the magnifying glass's lens.

CLUES

Common and Special Cause Variation



Types of Capability Indices



- Cr
- Cp
- Cpk
- Cpu
- Cpl
- Cpm
- Pr
- Pp
- Ppk
- Ppu
- Ppl

Symbols and Formulas



Symbols and Formulas



- Sigma-e = estimated sigma $\hat{\sigma}_e = \frac{\bar{R}}{d_2}$
- Sigma-i = standard deviation of the individual readings
(Excel uses the STDEV function) $\hat{\sigma}_i = \sqrt{\frac{\sum (X_i - \bar{X})^2}{n-1}}$

Symbols and Formulas - Cp



$$C_p = \frac{USL - LSL}{6 * \hat{\sigma}_e} = \frac{\text{Voice of the Customer}}{\text{Voice of the Process}}$$

Symbols and Formulas - Cp



$$C_p = \frac{USL - LSL}{6 * \hat{\sigma}_e}$$

Symbols and Formulas - Cp



- $C_p = 1.0$

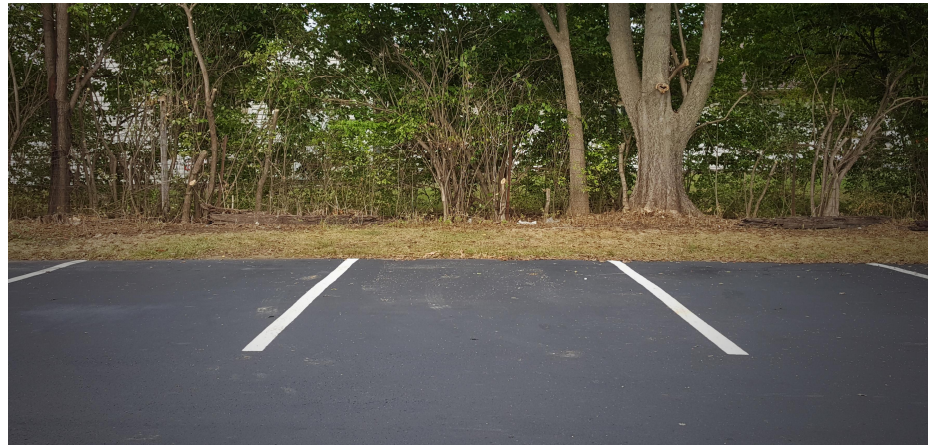


- The allowable spread is the same as the actual spread

Symbols and Formulas - C_p



- $C_p > 1$



- The allowable spread is wider than actual spread



Symbols and Formulas - C_p



- $C_p > 1$



- The vehicle *can* fit

Symbols and Formulas - C_p



- $C_p < 1.0$
- The space is too narrow



Symbols and Formulas



$$C_{pu} = \frac{(USL - \bar{X})}{(3 * \hat{\sigma}_e)}$$

$$C_{pl} = \frac{(\bar{X} - LSL)}{(3 * \hat{\sigma}_e)}$$

$C_{pk} = \text{Smaller of } C_{pu} \text{ and } C_{pl}$

Key Assumptions



- A control chart is completed
- The control chart shows no special causes
- One or both specifications exist
- The distribution of the data is bell-shaped

How Capability Analysis is Performed

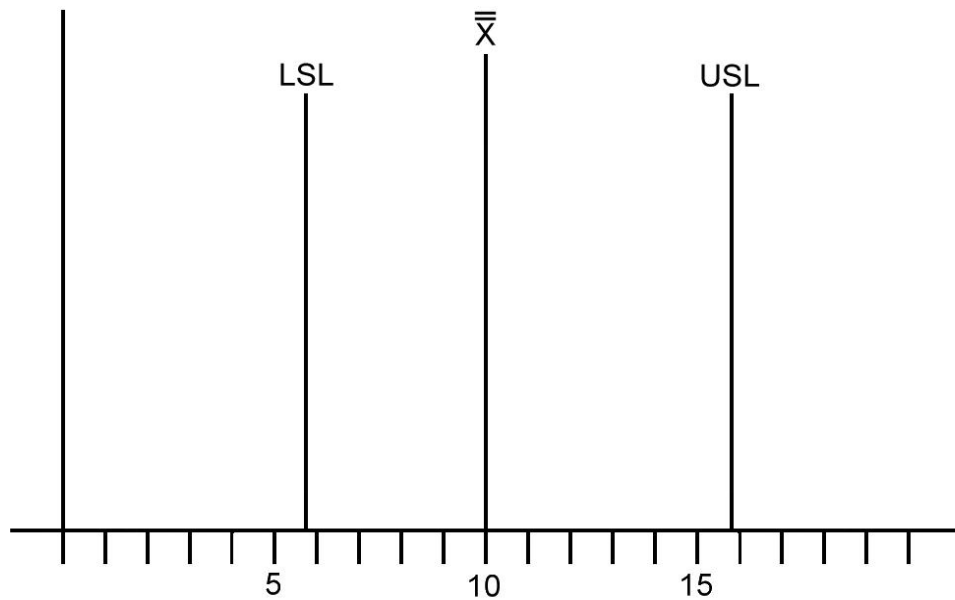


- Calculate the mean and the standard deviation
- Sketch the distribution & specification line(s)
- Calculate Z-values
- Determine expected percent out-of-spec
- Calculate the C_p , C_{pk} and/or P_p , P_{pk}

How Capability Analysis is Performed



- Sketch the distribution (optional, but helpful)



$$\begin{aligned}\bar{X} &= 10.0 \\ \bar{R} &= 5.81 \\ \text{USL} &= 15.8 \\ \text{LSL} &= 5.73 \\ n &= 5\end{aligned}$$

How Capability Analysis is Performed



- Calculate the standard deviation

$$\text{Estimated sigma} = \frac{\bar{R}}{d_2}$$

$$\text{Est. sigma} = \frac{5.81}{2.326} \sim 2.50$$

$$3 \times \text{sigma} = 7.50$$

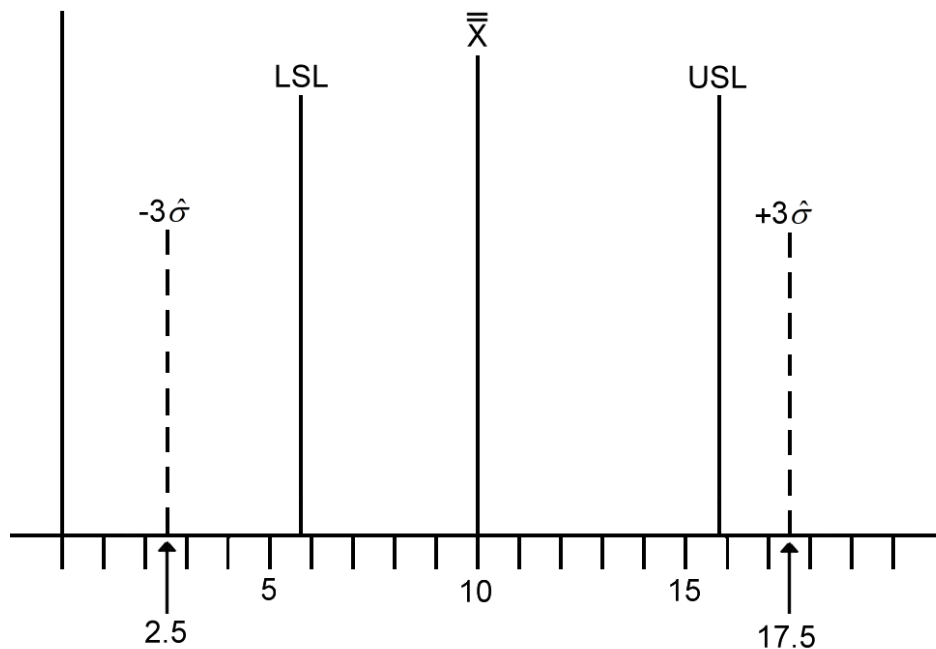
$$\text{Mean} \pm 3\text{sigma} = 17.50, 2.50$$

Subgroup size	d_2 values
2	1.128
3	1.693
4	2.059
5	2.326
6	2.534
7	2.704
8	2.847
9	2.970
10	3.078

How Capability Analysis is Performed



- Sketch the distribution (optional, but helpful)

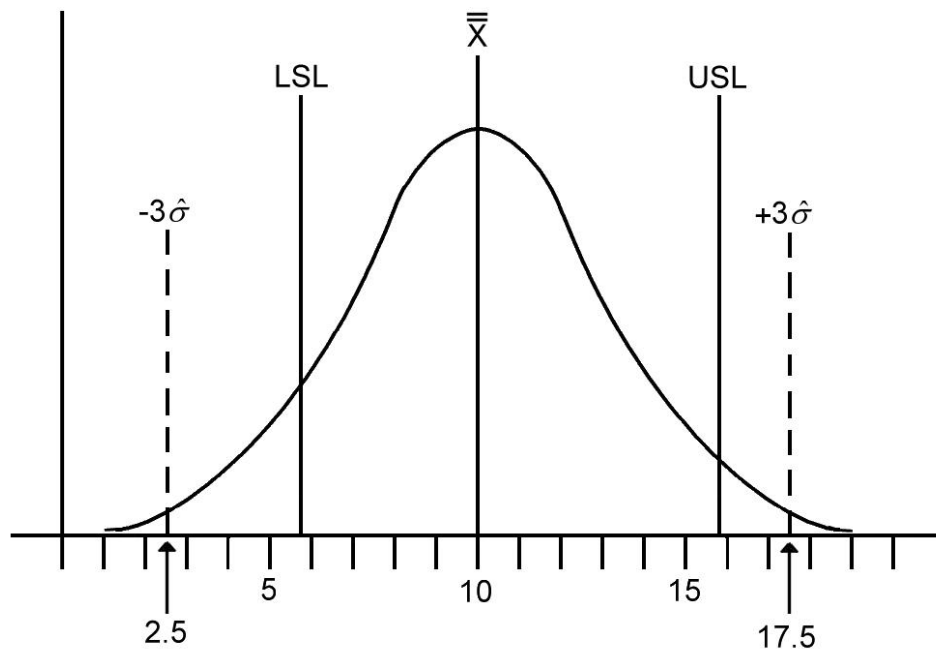


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How Capability Analysis is Performed



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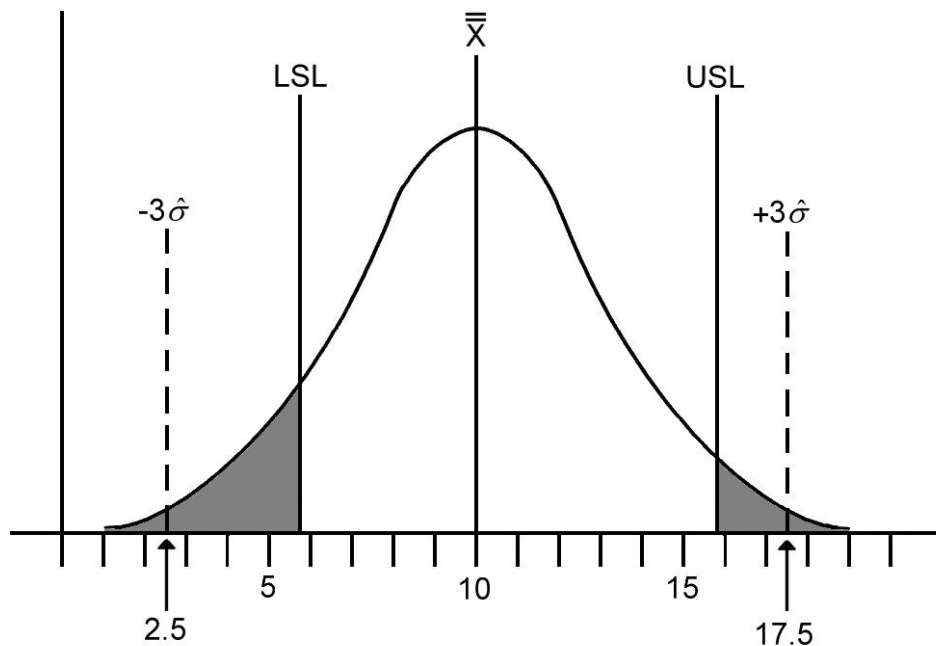


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How Capability Analysis is Performed



- Sketch the distribution (optional, but helpful)



$$\begin{aligned}\bar{X} &= 10.0 \\ \bar{R} &= 5.81 \\ USL &= 15.8 \\ LSL &= 5.73 \\ n &= 5\end{aligned}$$

How Capability Analysis is Performed



- Calculate Z_{upper} and Z_{lower}

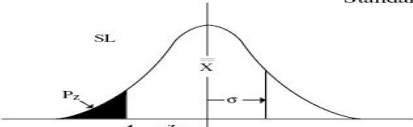
$$Z_{upper} = \frac{(\text{USL} - \text{Mean})}{\text{sigma}} = \frac{(15.8 - 10.0)}{2.50} = 2.32$$

$$Z_{lower} = \frac{(\text{Mean} - \text{LSL})}{\text{sigma}} = \frac{(10 - 5.73)}{2.50} = \sim 1.71$$

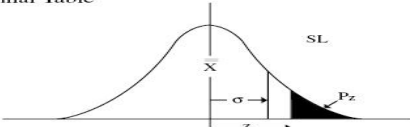
Standard Normal Table



Standard Normal Table

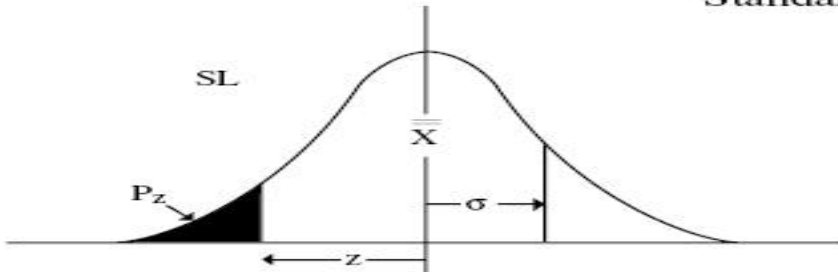


or

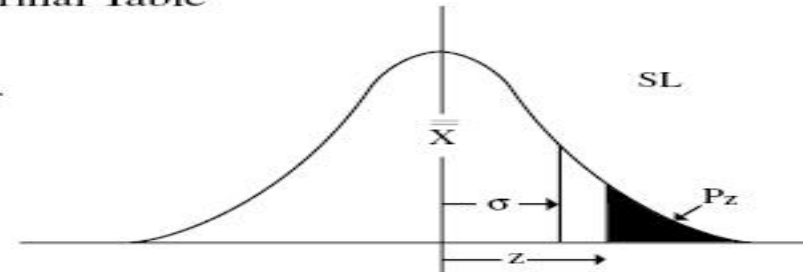


z	x.x0	x.x1	x.x2	x.x3	x.x4	x.x5	x.x6	x.x7	x.x8	x.x9
4.0	.00003									
3.9	.00005	.00005	.00004	.00004	.00004	.00004	.00004	.00004	.00003	.00003
3.8	.00007	.00007	.00007	.00006	.00006	.00006	.00006	.00005	.00005	.00005
3.7	.00011	.00010	.00010	.00010	.00009	.00009	.00008	.00008	.00008	.00008
3.6	.00016	.00015	.00015	.00014	.00014	.00013	.00013	.00012	.00012	.00011
3.5	.00023	.00022	.00022	.00021	.00020	.00019	.00019	.00018	.00017	.00017
3.4	.00034	.00032	.00031	.00030	.00029	.00028	.00027	.00026	.00025	.00024
3.3	.00048	.00047	.00045	.00043	.00042	.00040	.00039	.00038	.00036	.00035
3.2	.00069	.00066	.00064	.00062	.00060	.00058	.00056	.00054	.00052	.00050
3.1	.00097	.00094	.00090	.00087	.00084	.00082	.00079	.00076	.00074	.00071
3.0	.00135	.00131	.00126	.00122	.00118	.00114	.00111	.00107	.00104	.00100
2.9	.0019	.0018	.0018	.0017	.0016	.0016	.0015	.0015	.0014	.0014
2.8	.0026	.0025	.0024	.0023	.0023	.0022	.0021	.0021	.0020	.0019
2.7	.0035	.0034	.0033	.0032	.0031	.0030	.0029	.0028	.0027	.0026
2.6	.0047	.0045	.0044	.0043	.0041	.0040	.0039	.0038	.0037	.0036
2.5	.0062	.0060	.0059	.0057	.0055	.0054	.0052	.0051	.0049	.0048
2.4	.0082	.0080	.0078	.0075	.0073	.0071	.0069	.0068	.0066	.0064
2.3	.0107	.0104	.0102	.0099	.0096	.0094	.0091	.0089	.0087	.0084
2.2	.0139	.0136	.0132	.0129	.0125	.0122	.0119	.0116	.0113	.0110
2.1	.0179	.0174	.0170	.0166	.0162	.0158	.0154	.0150	.0146	.0143
2.0	.0228	.0222	.0217	.0212	.0207	.0202	.0197	.0192	.0188	.0183
1.9	.0287	.0281	.0274	.0268	.0262	.0256	.0250	.0244	.0239	.0233
1.8	.0359	.0351	.0344	.0336	.0329	.0322	.0314	.0307	.0301	.0294
1.7	.0446	.0436	.0427	.0418	.0409	.0401	.0392	.0384	.0375	.0367
1.6	.0548	.0537	.0526	.0516	.0505	.0495	.0485	.0475	.0465	.0455
1.5	.0668	.0655	.0643	.0630	.0618	.0606	.0594	.0582	.0571	.0559
1.4	.0808	.0793	.0778	.0764	.0749	.0735	.0721	.0708	.0694	.0681
1.3	.0968	.0951	.0934	.0918	.0901	.0885	.0869	.0853	.0838	.0823
1.2	.1151	.1131	.1112	.1093	.1075	.1056	.1038	.1020	.1003	.0985
1.1	.1357	.1335	.1314	.1292	.1271	.1251	.1230	.1210	.1190	.1170
1.0	.1587	.1562	.1539	.1515	.1492	.1469	.1446	.1423	.1401	.1379
0.9	.1841	.1814	.1788	.1762	.1736	.1711	.1685	.1660	.1635	.1611
0.8	.2119	.2090	.2061	.2033	.2005	.1977	.1949	.1922	.1894	.1867
0.7	.2420	.2389	.2358	.2327	.2297	.2266	.2236	.2206	.2177	.2148
0.6	.2743	.2709	.2676	.2643	.2611	.2578	.2546	.2514	.2483	.2451
0.5	.3085	.3050	.3015	.2981	.2946	.2912	.2877	.2843	.2810	.2776
0.4	.3446	.3409	.3372	.3336	.3300	.3264	.3228	.3192	.3156	.3121
0.3	.3281	.3283	.3245	.3207	.3169	.3132	.3094	.3057	.3020	.2983
0.2	.4207	.4168	.4129	.4090	.4052	.4013	.3974	.3936	.3897	.3859
0.1	.4602	.4562	.4522	.4483	.4443	.4404	.4364	.4325	.4286	.4247
0.0	.5000	.4960	.4920	.4880	.4840	.4801	.4761	.4721	.4681	.4641

Standard Normal Table



or



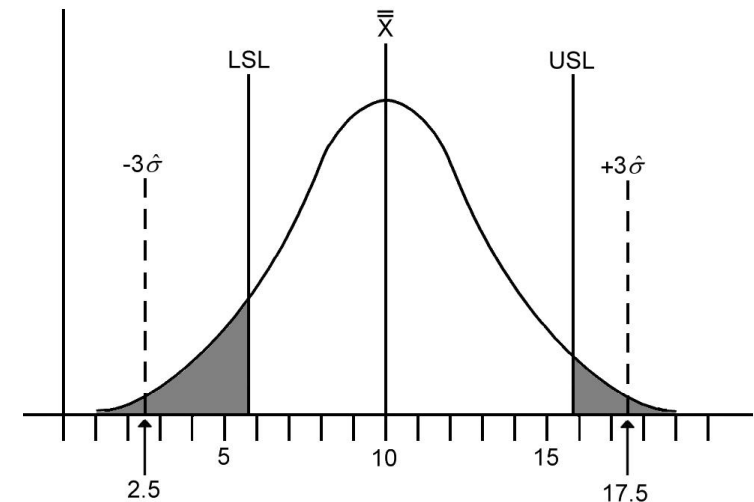
z	x.x0	x.x1	x.x2	x.x3	x.x4	x.x5	x.x6	x.x7	x.x8	x.x9
4.0	.00003									
3.9	.00005	.00005	.00004	.00004	.00004	.00004	.00004	.00004	.00003	.00003
3.8	.00007	.00007	.00007	.00006	.00006	.00006	.00006	.00005	.00005	.00005
3.7	.00011	.00010	.00010	.00010	.00009	.00009	.00008	.00008	.00008	.00008
3.6	.00016	.00015	.00015	.00014	.00014	.00013	.00013	.00012	.00012	.00012
3.5	.00023	.00022	.00022	.00021	.00020	.00019	.00019	.00018	.00017	.00017
3.4	.00034	.00032	.00031	.00030	.00029	.00028	.00027	.00026	.00025	.00025
3.3	.00048	.00047	.00045	.00043	.00042	.00040	.00039	.00038	.00036	.00036
3.2	.00069	.00066	.00064	.00062	.00060	.00058	.00056	.00054	.00052	.00052
3.1	.00097	.00094	.00090	.00087	.00084	.00082	.00079	.00076	.00074	.00074
3.0	.00135	.00131	.00126	.00122	.00118	.00114	.00111	.00107	.00104	.00104
2.9	.0019	.0018	.0018	.0017	.0016	.0016	.0015	.0015	.0014	.0014
2.8	.0026	.0025	.0024	.0023	.0023	.0022	.0021	.0021	.0020	.0020
2.7	.0035	.0034	.0033	.0032	.0031	.0030	.0029	.0028	.0027	.0027
2.6	.0047	.0045	.0044	.0043	.0041	.0040	.0039	.0038	.0037	.0037
2.5	.0062	.0060	.0059	.0057	.0055	.0054	.0052	.0051	.0049	.0049
2.4	.0082	.0080	.0078	.0075	.0073	.0071	.0069	.0068	.0066	.0066
2.3	.0107	.0104	.0102	.0099	.0096	.0094	.0091	.0089	.0087	.0087
2.2	.0139	.0136	.0132	.0129	.0125	.0122	.0119	.0116	.0113	.0113
2.1	.0179	.0174	.0170	.0166	.0162	.0158	.0154	.0150	.0146	.0146
2.0	.0228	.0222	.0217	.0212	.0207	.0202	.0197	.0192	.0188	.0188
1.9	.0287	.0281	.0274	.0268	.0262	.0256	.0250	.0244	.0239	.0239
1.8	.0359	.0351	.0344	.0336	.0329	.0322	.0314	.0307	.0301	.0301

How Capability Analysis is Performed



$$Z_{upper} = 2.32 \rightarrow 0.0102 \rightarrow 1.02\%$$

$$Z_{lower} = 1.71 \rightarrow 0.0436 \rightarrow 4.36\%$$



We expect 1.02% + 4.36% of data to be outside the specification limits.

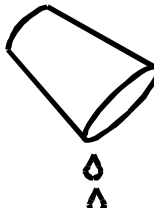
How Capability Analysis is Performed



- $C_p = \text{spec spread} / \text{process spread}$
- $C_p = (15.8 - 5.73) / (6 * 2.50)$
- $C_p = 0.67$

- $C_{pk} = \text{Smallest Z value} / 3$
- $C_{pk} = 1.71 / 3$
- $C_{pk} = 0.57$

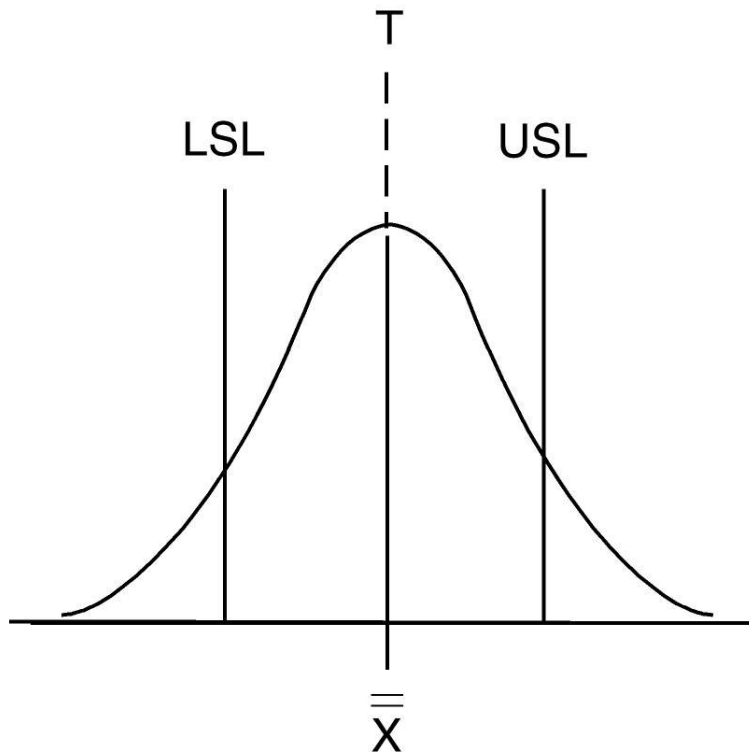
Getting the Most from Capability Analysis



$$C_{pm} = \frac{USL - LSL}{6 \hat{\sigma}_{C_{pm}}}$$

$$\hat{\sigma}_{C_{pm}} = \sqrt{\frac{\sum (X_i - T)^2}{n - 1}}$$

Average is at the Target Value

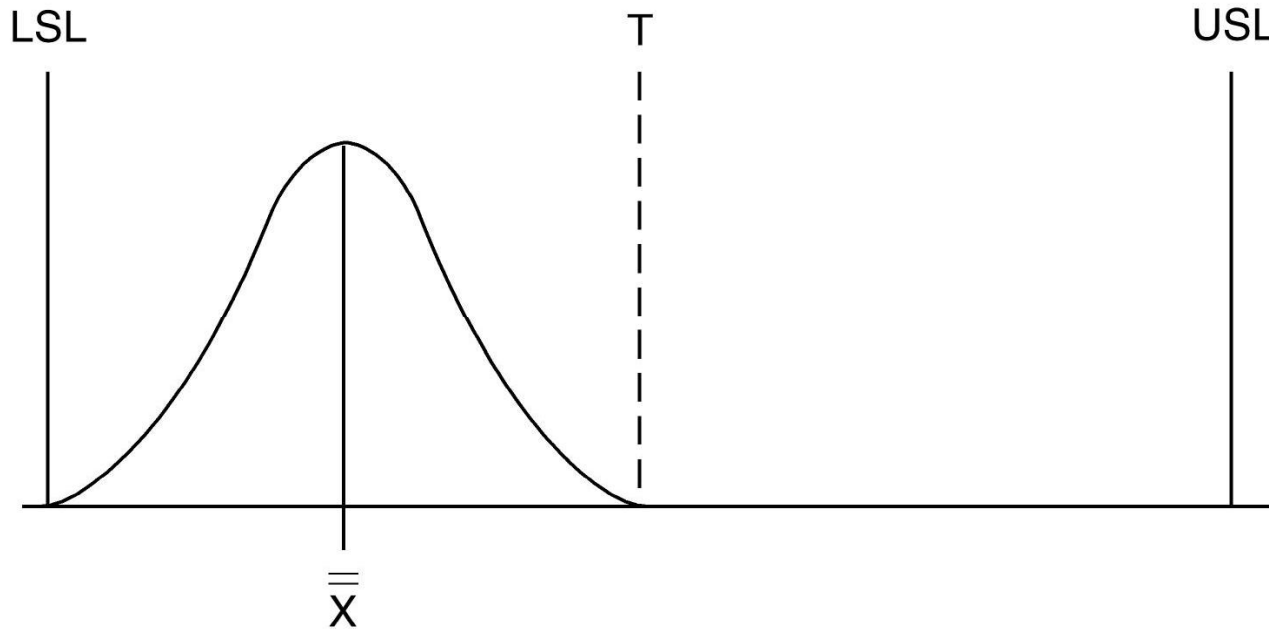


$$C_p = 0.5$$

$$C_{pk} = 0.5$$

$$C_{pm} = 0.5$$

Average is Off Target

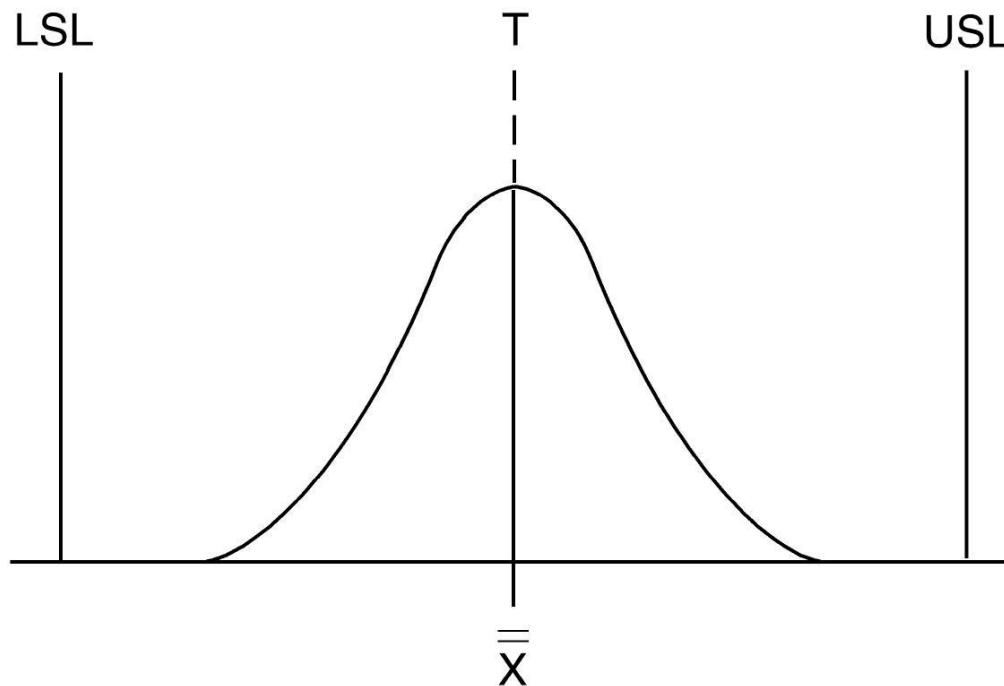


$$C_p = 2.0$$

$$C_{pk} = 1.0$$

$$C_{pm} = 0.65$$

Average is at the Target Value



$$C_p = 1.5$$
$$C_{pk} = 1.5$$
$$C_{pm} = 1.5$$

Final Thoughts



- Control charts are designed to provide stability information
- Capability analysis allows you to compare different processes
- Capability analysis brings together the process limits (± 3 sigma) and specification limits

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